



NEVADA INSTRUCTIONAL MATERIALS

FOR THE
NEVADA ACADEMIC CONTENT STANDARDS FOR MATHEMATICS

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Grade 4

TEACHER EDITION



Scoring Support Materials

Grade 4 Mathematics

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Introduction

This document represents the Phase III release of Nevada Instructional Materials. These released materials were developed in collaboration with Nevada educators, the Nevada Department of Education, and WestEd (a nonprofit research development and service agency).

These materials are intended for use in various guided instructional activities to support deep understanding of the Nevada Academic Content Standards (NVACS) for English Language Arts and mathematics based on Common Core. The Nevada Instructional Materials provide educators opportunities to investigate and explore the standards and tasks that are aligned to the standards. The Nevada educators involved in the development of these materials also developed “Teacher Tips” to assist in using these materials as an instructional resource. The Nevada Instructional Materials also provide educators opportunities to investigate and explore the standards and tasks that are aligned to the standards.

While these materials can provide students with practice in responding to a variety of assessment items, it is more important that they are used to help students deepen their understanding of the expectations embedded in the standards. If these instructional materials are used solely as an assessment practice activity, we highly recommend that educators go over each item with their students and evaluate each answer choice so that students can better understand the knowledge required to successfully complete each task.

Through rich classroom discussion around each item and the various answer choices or potential responses, educators can actively engage students in critical thinking, reasoning, and application of knowledge and skills, helping to ensure all students are ready for success in the 21st century.



Item Level Data

Item Number	NVACS*	DOK	Answers
1	4.OA.A1	1	A
2	4.OA.A3	2	-----
3	4.OA.A2	2	-----
4	4.OA.A3	3	-----
5	4.OA.B4	1	C
6	4.OA.C5	2	A, D
7	4.OA.C5	2	-----
8	4.NBT.A2	1	-----
9	4.NBT.A3	1	-----
10	4.NBT.A1	1	B
11	4.NBT.B4	1	B, C
12	4.NBT.B5	1	A
13	4.NBT.B6	1	-----
14	4.NBT.B5	2	-----
15	4.NF.A1	1	B, D, E
16	4.NF.A2	2	B
17	4.NF.A2	3	-----
18	4.NF.A2	2	A, C, D
19	4.NF.B3b	1	B, E, F
20	4.NF.B3c	1	-----
21	4.NF.B3d	1	A, D
22	4.NF.B3d	2	-----
23	4.NF.B4a	1	D

Item Number	NVACS*	DOK	Answers
24	4.NF.B4b	2	-----
25	4.NF.B4c	2	-----
26	4.NF.B4c	3	-----
27	4.NF.C5	1	-----
28	4.NF.C6	1	C
29	4.NF.C6	1	-----
30	4.NF.C7	2	-----
31	4.MD.A1	1	-----
32	4.MD.A2	2	D
33	4.MD.A2	3	-----
34	4.MD.A3	2	A, B, D, F
35	4.MD.B4	2	-----
36	4.MD.C5a	1	C
37	4.MD.C7	1	B, C, E
38	4.MD.C6	2	-----
39	4.G.A1	1	B, E, H
40	4.G.A1	2	-----
41	4.G.A2	1	D
42	4.G.A2	1	B, F
43	4.G.A2	3	-----
44	4.G.A3	1	A, C, D, E
45	4.G.A3	2	-----

*Nevada Academic Content Standards

**Detailed objectives for Content Standards and Depth of Knowledge (DOK) descriptions
can be found on the Nevada Department of Education web site.**



**Scoring Guides
and
Student Response
Examples by
Score Point**

**Grade 4
Mathematics**

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.OA.A1

1 A statement is shown below.

The number 48 is 6 times as many as 8 .

Which equation is represented by the statement?

- A $6 \times 8 = 48$
- B $6 + 8 = 48$
- C $48 - 6 = 8$
- D $48 \times 6 = 8$

Scoring Notes:

Rationale A: correct

Rationale B: shows 6 more than 8, which is not 48

Rationale C: shows 6 less than 48, which is not 8

Rationale D: shows 48 times 6, which is not 8

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.OA.A3

2 Lonnie buys 8 cases of bottled water. Each case contains 24 bottles of water. Lonnie puts all but 15 of the bottles of water into coolers. How many bottles of water does Lonnie put into coolers? Write the answer in the blank below.

_____ bottles of water

Scoring Notes:

177 (bottles of water)

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.OA.A2

3

All of the baseball hats at a store went on sale.

- The number of hats sold on Thursday was 12 .
- The number of hats sold on Friday was 2 times as great as the number of hats sold on Thursday.
- The number of hats sold on Saturday was 3 times as great as the number of hats sold on Friday.

Select true or false for each statement below about the numbers of hats sold on different days.

A The number of hats sold on Saturday is 6 times as great as the number of hats sold on Thursday.

True False

B The number of hats sold on Friday is 8 times as great as the number of hats sold on Saturday.

True False

C The number of hats sold on Friday is 24 .

True False

D The number of hats sold on Saturday is 96 .

True False

E The total number of hats sold on Friday, Saturday, and Sunday is 108 .

True False

Scoring Notes:

True: A, C, E

False: B, D

Rationale B: multiplies 12×2 and sees that 24 is 8 times as great as 3

Rationale D: multiplies 12×6 but then adds 12×2

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.OA.A3

- 4** A roller skating rink rents pairs of roller skates to its visitors.
- The rink has 36 visitors on Friday.
 - 11 visitors are **not** roller skating.
- A** Each roller skate in a pair has 4 wheels. What is the total number of wheels on the roller skates of the visitors who are roller skating? Show your work or explain your thinking.

The roller skating rink keeps 300 pairs of roller skates to rent to visitors.

- On Saturday morning, 42 pairs of roller skates are rented for the entire day.
 - On Saturday afternoon, 4 groups visit the roller skating rink.
 - Each group has 16 children who need to rent pairs of roller skates.
- B** After all of the children have rented their roller skates, how many pairs of roller skates does the roller skating rink have remaining to rent? Show your work or explain your thinking.

Write your response on the grid on the next page.

Scoring Notes:

Score	Description
3	Student scores 3 points.
2	Student scores 2–2.5 points.
1	Student scores 0.5–1.5 points.
0	Student’s response provides insufficient evidence of appropriate skills or knowledge to successfully accomplish the task.
Blank	No student response.

Score Points

Part A:	score 1.5 points	correct answer with correct and complete work or explanation
	OR	
	score 1.0 point	correct answer with partially correct work or incomplete explanation
	OR	incorrect answer due to a calculation error (work must be shown)
	OR	
	score 0.5 point	correct answer with no work or explanation
	OR	partially correct or incomplete explanation
	OR	some correct procedure
Part B:	score 1.5 points	correct answer with correct and complete work or explanation
	OR	
	score 1.0 point	correct answer with partially correct work or incomplete explanation
	OR	incorrect answer due to a calculation error (work must be shown)
	OR	incorrect answer due to correct but incomplete procedure (work or explanation must be shown/included)
	OR	
	score 0.5 point	correct answer with no work or explanation
	OR	partially correct or incomplete explanation
	OR	some correct procedure
	OR	
	score 0.5 point	correct answer with no work or explanation
	OR	partially correct or incomplete explanation
	OR	some correct procedure

Correct Answers

Part A: 200 (wheels)

$$36 - 11 = 25$$

$$25 \times 2 \times 4 = 200$$

or equivalent work

OR

Sample Explanation:

When 11 of the 36 people are not roller skating, then 25 people will be roller skating. Each skate has 4 wheels and each person has 2 skates, so each person's skates have a total of 8 wheels.

$8 \times 25 = 200$. There are a total of 200 wheels.

Part B: 194 (pairs)

$$300 - 42 = 258$$

$$4 \times 16 = 64$$

$$258 - 64 = 194$$

or equivalent work

OR

Sample Explanation:

Subtract 42 pairs of roller skates from 300 pairs of skates to find out how many pairs of skates are still to be rented. There are 258 pairs of skates that can be rented. There are 4 groups of 16 children, so multiply 16 by 4 to find out how many roller skates are now rented, $16 \times 4 = 64$.

Subtract 64 from the number of skates left to rent, $258 - 64 = 194$. The roller rink has 194 pairs of skates that can be rented.

Instructional Materials Question 4

A	$\begin{array}{r} 36 \\ - 11 \\ \hline 25 \end{array}$	<p>The total number of wheels is 200. I know this because I used multiplication and subtraction. First, I subtracted 36 and 11 to get 25 visitors. Then, I multiplied 25 and 4 to get a product of 100. I know people have two feet so I multiplied 100 and 2 to get a product of 200.</p>		
	$\begin{array}{r} 25 \\ \times 4 \\ \hline 100 \end{array}$			
	$\begin{array}{r} 100 \\ \times 2 \\ \hline 200 \end{array}$			
B	$\begin{array}{r} 29 \\ 300 \\ - 42 \\ \hline 258 \end{array}$	$\begin{array}{r} 16 \\ \times 4 \\ \hline 64 \end{array}$	$\begin{array}{r} 258 \\ - 64 \\ \hline 194 \end{array}$	<p>There are 194 remaining roller skates. I know this because I used subtraction and multiplication. First I subtracted 300 and 42 to get 258. Then I multiplied 16 and 4 to get a product of 64. I subtracted 258 and 64 to get 194 remaining roller skates.</p>

Score Point: 3

The response to Part A includes the correct answer with correct and complete explanation (1.5).

The response to Part B includes the correct answer with correct and complete explanation (1.5).

Instructional Materials Question 4

- A** The total number of wheels on the roller skates being used by visitors is 200 wheels. I know that because 36 visitors came on Friday, and only 25 visitors were skating. There is 4 wheels on each roller skate in a pair, so including just 1 skate per visitor that is skating, there would be 100 wheels. Add one more skate to the visitors that are skating to make a pair, so that would make 100 more wheels. All the wheels together is 200 wheels.
- B** The roller skating rink has 194 pairs of skates left to rent. I know that because 300 pairs of skates minus 42 pairs of roller skates is 258 pairs of roller skates. 4 more groups came with 16 children each who needed a pair of roller skates. Sixteen multiplied by four is 64, so the rink then has 194 pairs of roller skates left.

Score Point: 3

The response to Part A includes the correct answer with correct and complete explanation (1.5).

The response to Part B includes the correct answer with correct and complete explanation (1.5).

Instructional Materials Question 4

A

$$\begin{array}{r} 36 \\ - 11 \\ \hline 25 \end{array}$$

$$\begin{array}{r} 2 \\ 25 \\ \times 4 \\ \hline 100 \end{array}$$

There are
100 total wheels.

B

$$\begin{array}{r} 239 \\ - 42 \\ \hline 258 \end{array}$$

$$\begin{array}{r} 2 \\ 16 \\ \times 4 \\ \hline 64 \end{array}$$

$$\begin{array}{r} 1258 \\ - 64 \\ \hline 1194 \end{array}$$

194 roller skates
are left.

Score Point: 2

The response to Part A includes some correct procedure (0.5). The response to Part B includes the correct answer with correct and complete work (1.5).

Instructional Materials Question 4

A If there are there are 36 visitors, and 11 are not skating at the roller skating rink, and there are 8 wheels in a pair of skates, there are 200 wheels on the roller rink because 36 minus 11 equals 25, and 25 multiplied by 8 equals 200.

B After all the children rented their roller skates, there are still 236 that can be rented from the skating rink because if 4 groups visit, and 16 children from each group rent a pair, 64 pairs are rented in all, and the skating rink has a total of 300 pairs of roller skates, and 300 minus 64 is 236.

Score Point: 2

The response to Part A includes the correct answer with correct and complete explanation (1.5). The response to Part B includes an incorrect answer due to correct but incomplete procedure (explanation included) (1.0).

Instructional Materials Question 4

A

$$\begin{array}{r} 36 \\ - 11 \\ \hline 25 \\ \times 4 \\ \hline 100 \end{array}$$

100 wheels

The total number of wheels is 100. I know this because I multiplied and subtracted. First, I subtracted 11 from 36 and got 25. Then I multiplied 25 and 4 with a product of 100.

B

$$\begin{array}{r} 16 \\ \times 4 \\ \hline 64 \\ 300 - 64 \\ \hline 236 \end{array}$$

The roller skating rink has 236 more roller skates to rent. I know this because I multiplied and subtracted. First, I multiplied 16 and 4 which equals 64. Then I subtracted 64 from 300 and got 236.

Score Point: 1

The response to Part A includes some correct procedure (0.5). The response to Part B includes an incorrect answer due to correct but incomplete procedure (explanation included) (1.0).

Instructional Materials Question 4

A

3	6	
-	1	1
25		

$25 \times 4 = 100$ wheels

First I took 36 minus 11 because 11 visitors are not skating. I come up with 25 people who are skating. Then, since there are 4 wheels on each I timesed 25 x 4 to get 100.

B

3 ³	0 ⁰	0 ⁰
-	4	2
258		
-	1	6
242		

242 skates

So first I took how many skates they had, 300. I subtracted 42 since they were gone. After I subtracted 16 because of children. Then I got 242.

Score Point: 1

The response to Part A includes some correct procedure (0.5). The response to Part B includes some correct procedure (0.5).

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.OA.B4

5

In which list are **all** the numbers prime?

- A 5 45 85
- B 6 38 92
- C 17 31 83
- D 19 63 97

Scoring Notes:

Rationale A: all end in 5; only 5 is prime

Rationale B: confused prime and composite

Rationale C: correct

Rationale D: 63 is composite

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.OA.C5

6 A pattern of figures that uses squares is described below.

- The first figure in the pattern has 2 squares.
- The next figure in the pattern is always found by adding 3 squares to the number of squares in the figure before it.

Which of these make the statement below about the number of squares in each figure in the pattern true? Select **all** that apply.

The number of squares in each figure in the pattern _____.

- A** can be odd or even
- B** is always odd
- C** is always even
- D** can be prime or composite
- E** is a multiple of 2
- F** is a multiple of 3
- G** can be evenly divided by 5

Scoring Notes:

Correct answers: A, D

Rationale B: number added is odd

Rationale C: first term is even

Rationale E: true for every other term

Rationale F: misinterprets impact of number added

Rationale G: true for some terms, but not all

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.OA.C5

7

Allie created a number pattern starting with the number 13 and following the rule “add 5 .”

Write the first six numbers in Allie’s pattern in the spaces below.

Explain why the digit in the ones place of each number in Allie’s pattern can be only one of two different digits.

Write your response on the grid below.

Scoring Notes:

For this item, a full-credit response (2 points) includes

- correct first six numbers in the pattern, 13, 18, 23, 28, 33, 38
- AND**
- explanation indicating why the digit in the ones place of each number in the pattern can be only one of two different digits

For example,

- The first number has a 3 in the ones place, so one of the digits is 3 . By adding 5, you get 18, so the other digit is 8 . The next “add 5” would actually be the same as adding 10 to the starting number, and by adding 10 the ones place in the two numbers would be the same. Then adding 5 again would make an 8 in the ones place. Since you’re adding by 5s and 10s only, the ones digit can only be one of two different digits in the pattern.

For this item, a partial-credit response (1 point) includes

- correct first six numbers in the pattern, 13, 18, 23, 28, 33, 38
- OR**
- some explanation indicating why the digit in the ones place of each number in the pattern can be only one of two different digits

For this item, a no-credit response (0 points) includes none of the features of a full- or partial-credit response.

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.NBT.A2

8

Select true or false for **each** number sentence represented below.

A $342 < 336$

True False

B 43 ones $>$ 5 tens

True False

C $100 + 40 + 6 < 147$

True False

D 28 tens + 24 ones $>$ 29 tens + 13 ones

True False

Scoring Notes:

True: C, D

False: A, B

Rationale A: only compares digit in ones place

Rationale B: only compares whole numbers, but not place value

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.NBT.A3

9

A number is shown below.

594,687

Complete the table below by writing the value of the number when rounded to **each** place.

	594,687
Rounded to hundreds place	
Rounded to millions place	
Rounded to ten-thousands place	
Rounded to thousands place	

Scoring Notes:

	594,687
Rounded to hundreds place	594,700
Rounded to millions place	1,000,000
Rounded to ten-thousands place	590,000
Rounded to thousands place	595,000

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.NBT.A1

10

Look at the two numbers below.

206 63

Which statement about the place value of the 6 in both numbers is true?

- A** The value of the 6 in 63 is the same as the value of the 6 in 206 .
- B** The value of the 6 in 63 is 10 times as great as the value of the 6 in 206 .
- C** The value of the 6 in 206 is 10 times as great as the value of the 6 in 63 .
- D** The value of the 6 in 206 is 100 times as great as the value of the 6 in 63 .

Scoring Notes:

Rationale A: thinks of single digit 6, not place value

Rationale B: correct

Rationale C: opposite is true

Rationale D: thinks of 100 times since 206 is a 3-digit number

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.NBT.B4

11 Which equations are true? Select **all** that apply.

A $518 + 79 = 587$

B $518 - 79 = 439$

C $5892 + 317 = 6209$

D $5892 - 317 = 5585$

Scoring Notes:

Correct answers: B, C

Rationale A: did not regroup

Rationale D: subtracted lesser digit from greater digit in each place value

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.NBT.B5

12 Which expression could be used to find the product of 5,039 and 8 ?

A $(5,000 \times 8) + (30 \times 8) + (9 \times 8)$

B $(500 \times 8) + (30 \times 8) + (9 \times 8)$

C $(5,000 \times 8) + (300 \times 8) + (9 \times 8)$

D $(5 \times 8) + (3 \times 8) + (9 \times 8)$

Scoring Notes:

Rationale A: correct

Rationale B: uses 500 for place value of 5 instead of 5,000

Rationale C: uses 300 for place value of 3 instead of 30

Rationale D: ignores all place values

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.NBT.B6

13 Maggie has 150 beads. She puts an equal number of the beads into each of 7 boxes. How many beads are remaining? Write the answer in the blank below.

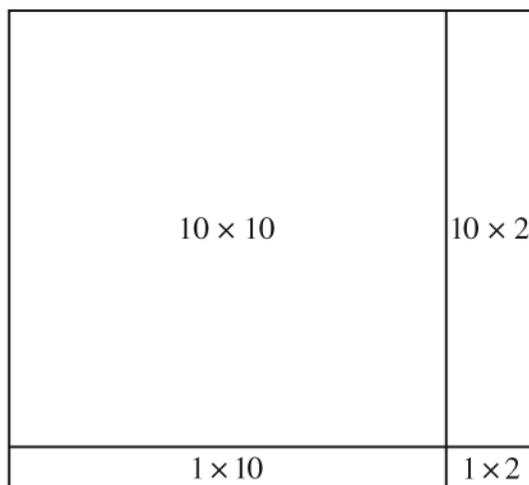
_____ beads remaining

Scoring Notes:

3 (beads remaining)

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.NBT.B5

14 The diagram below models the product of 2 factors.



What are the 2 factors modeled by the diagram?

Find the product modeled by the diagram. Show your work.

Write your response on the grid below.

Scoring Notes:

For this item, a full-credit response (2 points) includes

- correct two factors modeled by the diagram, 11 and 12
- AND**
- correct work identifying the product modeled by the diagram

For example,

$$11 \times 12$$

$$10 \times 12 = 120$$

$$1 \times 12 = 12$$

$$120 + 12 = 132$$

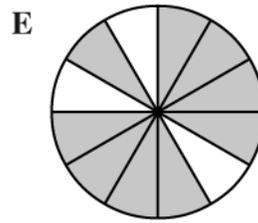
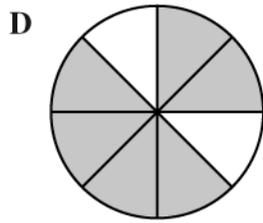
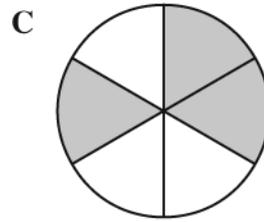
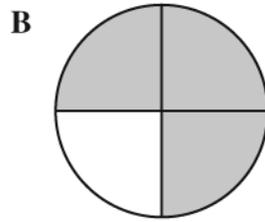
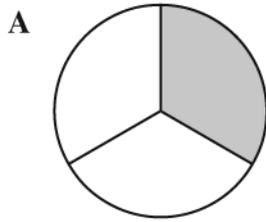
For this item, a partial-credit response (1 point) includes

- correct two factors modeled by the diagram, 11 and 12
- OR**
- incorrect product based on a calculation error (work identifying the product modeled by the diagram must be shown)

For this item, a no-credit response (0 points) includes none of the features of a full- or partial-credit response.

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.NF.A1

15 Which pictures are shaded to model a fraction that is equivalent to $\frac{3}{4}$? Select **all** that apply.



Scoring Notes:

Correct answers: B, D, E

Rationale A: $4 - 3 = 1$, $\frac{1}{3}$ shaded

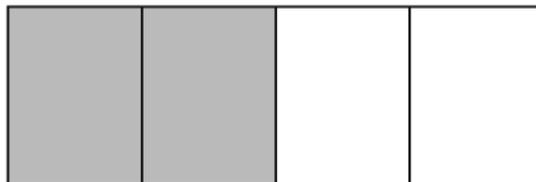
Rationale C: 3 sections shaded, but out of 6

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.NF.A2

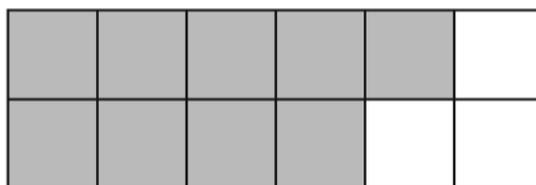
16

Two equal-sized rectangles, shown below, are shaded to model $\frac{2}{4}$ and $\frac{9}{12}$.

Rectangle 1



Rectangle 2



Which statement about the shaded amount of each rectangle is true?

- A Since $\frac{2}{4} = \frac{1}{2}$ and $\frac{9}{12} > \frac{1}{2}$, the shaded amount of rectangle 1 is greater than the shaded amount of rectangle 2.
- B Since $\frac{2}{4} = \frac{1}{2}$ and $\frac{9}{12} > \frac{1}{2}$, the shaded amount of rectangle 1 is less than the shaded amount of rectangle 2.
- C Since $\frac{2}{4} > \frac{1}{2}$ and $\frac{9}{12} < \frac{1}{2}$, the shaded amount of rectangle 1 is greater than the shaded amount of rectangle 2.
- D Since $\frac{2}{4} > \frac{1}{2}$ and $\frac{9}{12} < \frac{1}{2}$, the shaded amount of rectangle 1 is less than the shaded amount of rectangle 2.

Scoring Notes:

Rationale A: misinterprets comparisons to $\frac{1}{2}$

Rationale B: correct

Rationale C: incorrect comparisons to $\frac{1}{2}$

Rationale D: incorrect comparisons to $\frac{1}{2}$, misinterprets comparisons

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.NF.A2

17

Aaron, Maria, and Cody are reading the same book.

- Aaron has read $\frac{7}{10}$ of the pages in the book.
- Maria has read $\frac{5}{8}$ of the pages in the book.
- Cody has read $\frac{2}{3}$ of the pages in the book.

A Maria says that she has read a greater fraction of the pages in the book than Aaron has read. Is Maria correct? Show your work **and** explain your thinking.

B Write a number sentence, using $>$, $=$, or $<$, that compares the fraction of the pages in the book that Aaron has read to the fraction of the pages in the book that Cody has read. Show or explain how you know your comparison is true.

Write your response on the grid on the next page.

Scoring Notes:

Score	Description
4	Student scores 4 points.
3	Student scores 3–3.5 points.
2	Student scores 2–2.5 points.
1	Student scores 0.5–1.5 points.
0	Student’s response provides insufficient evidence of appropriate skills or knowledge to successfully accomplish the task.
Blank	No student response.

Score Points

Part A:	score 2.0 points	correct answer with correct and complete work and correct and complete explanation
	OR	
	score 1.5 points	correct answer with correct work and partially correct or incomplete explanation
	OR	
	score 1.0 point	correct answer with partially correct work and partially correct or incomplete explanation
	OR	
	score 0.5 point	correct answer with partially correct work and no explanation
	OR	partially correct or incomplete explanation
	OR	some correct procedure
Part B:	score 2.0 points	correct number sentence with correct and complete work or explanation
	OR	
	score 1.5 points	correct number sentence with partially correct work or incomplete explanation
	OR	incomplete number sentence with correct and complete work or explanation
	OR	
	score 1.0 point	correct number sentence with no work or explanation
	OR	partially correct or incomplete explanation
	OR	
	score 0.5 point	some correct procedure

Correct Answers

Part A: Maria is not correct.

$$\frac{7}{10} \times \frac{4}{4} = \frac{28}{40}$$

$$\frac{5}{8} \times \frac{5}{5} = \frac{25}{40}$$

$$\frac{28}{40} > \frac{25}{40}$$

or equivalent work

AND

Sample Explanation:

Maria is not correct, because $\frac{7}{10}$ is equivalent to $\frac{28}{40}$, and $\frac{5}{8}$ is equivalent to $\frac{25}{40}$. Since the fractions have the same denominator, and 28 is greater than 25, $\frac{28}{40}$ is greater than $\frac{25}{40}$. So, Aaron has read a greater fraction of the pages in the book than Maria has read.

Part B: $\frac{7}{10} > \frac{2}{3}$

$$\frac{7}{10} = \frac{7 \times 3}{10 \times 3} = \frac{21}{30}$$

$$\frac{2}{3} = \frac{2 \times 10}{3 \times 10} = \frac{20}{30}$$

$$\frac{21}{30} > \frac{20}{30}$$

$$\frac{7}{10} > \frac{2}{3}$$

or equivalent work

OR

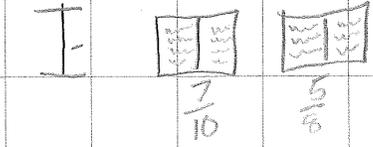
Sample Explanation:

Multiply $\frac{7}{10}$ by $\frac{3}{3}$ and $\frac{2}{3}$ by $\frac{10}{10}$ so that both fractions have the same denominator of 30. Since

$$\frac{21}{30} > \frac{20}{30}, \text{ then } \frac{7}{10} > \frac{2}{3}.$$

Instructional Materials Question 17

A V- Maria says she has read a greater fraction of the pages in the book than Aaron has read. Is Maria correct?

I- 

E- $\frac{7}{10} > \frac{5}{8}$ $\frac{7 \times 4}{10 \times 4} > \frac{5 \times 5}{8 \times 5}$ $\frac{28}{40} > \frac{25}{40}$

V

W- Maria is not correct because $\frac{7}{10}$ is greater than $\frac{5}{8}$. First I had to find a common denominator, $10 \times 4 = 40$ $8 \times 5 = 40$. So you multiply $7 \times 4 = 28$ $5 \times 5 = 25$, $\frac{28}{40} > \frac{25}{40}$. Therefore Maria is incorrect.

B V- Write a number sentence, using $>$, $=$, or $<$ that compares the fraction of the pages in the book that Aaron has read to the fraction of the page in the book Cody has read.

I- $\frac{7}{10}$  $\frac{2}{3}$ 

E- $\frac{7 \times 3}{10 \times 3} = \frac{21}{30}$ $\frac{2 \times 10}{3 \times 10} = \frac{20}{30}$

W- The comparison is true because $\frac{7}{10}$ is greater than $\frac{2}{3}$. First you have to find a common denominator. I multiplied $10 \times 3 = 30$ $3 \times 10 = 30$, $7 \times 3 = 21$ $2 \times 10 = 20$. So $\frac{21}{30} > \frac{20}{30}$. That's how I know the comparison is true.

Score Point: 4

The response to Part A includes the correct answer with correct and complete work and correct and complete explanation (2.0). The response to Part B includes a correct number sentence with correct and complete explanation (2.0).

Instructional Materials Question 17

A

V = Aaron, Maria, and Cody are reading the game book, Maria says she read more pgs than Aaron.

I = $\text{A} = \frac{7}{10} \text{ pg.}$ $\text{C} = \frac{5}{8} \text{ pg.}$

E = $\frac{7 \times 8 = 56}{10 \times 8 = 80}$ $\frac{5 \times 10 = 50}{8 \times 10 = 80}$

W = Maria says she read more pgs. than Aaron. I multiply the fact.
 ~~$(\frac{7 \times 8 = 56}{10 \times 8 = 80} \frac{5 \times 10 = 50}{8 \times 10 = 80})$. Maria was wrong, she read $\frac{50}{80}$, Aaron read $\frac{56}{80}$.~~

B

Aaron	Cody
$\frac{7 \times 3 = 21}{10 \times 3 = 30}$	$\frac{2 \times 10 = 20}{3 \times 10 = 30}$

$\frac{21}{30} > \frac{20}{30}$

$\frac{21}{30} = \text{aaron}$ $\frac{20}{30} = \text{Maria}$

Score Point: 3

The response to Part A includes the correct answer with correct and complete work and correct and complete explanation (2.0). The response to Part B includes a correct number sentence with correct work and partially correct explanation (1.5).

Instructional Materials Question 17

A)

$\frac{7}{10}$	$\times 4$	$\frac{28}{40}$		$\frac{5}{8}$	$\times 5$	$\frac{10}{40}$
		Aaron				Maria

maria is wrong because Aaron
read $\frac{28}{40}$ maria read $\frac{10}{40}$.

B)

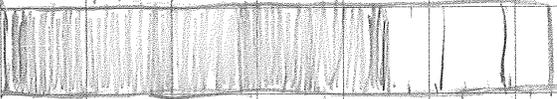
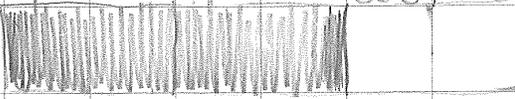
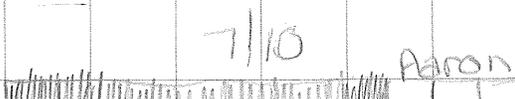
$\frac{7}{10}$	$\times 3$	$\frac{21}{30}$		$\frac{2}{3}$	$\times 10$	$\frac{20}{30}$
		Aaron				Cody

$\frac{21}{30}$ is 7 than $\frac{20}{30}$.

Score Point: 2

The response to Part A includes the correct answer with partially correct work (0.5). The response to Part B includes a correct number sentence with correct and complete work (2.0).

Instructional Materials Question 17

A	V-	maria read $\frac{5}{8}$ of the pages in the book Aaron read $\frac{7}{10}$ of the pages in the book.
		<p style="text-align: center;">maria $\frac{5}{8}$</p> 
I		<p style="text-align: center;">Aaron $\frac{7}{10}$</p> 
		<p>W- what I did is that I drew two boxes and put $\frac{5}{8}$ on top of one and $\frac{7}{10}$ on top of the other one. Then I filled in $\frac{7}{10}$ and $\frac{5}{8}$. I seen that they were equal. For my equation I put "$\frac{5}{8}$ is equal to $\frac{7}{10}$."</p>
	E	$\frac{5}{8}$ is equal to $\frac{7}{10}$
B	V-	Aaron read $\frac{7}{10}$ of the pages. Cody read $\frac{2}{3}$ of the pages
		<p style="text-align: center;">$\frac{2}{3}$ Cody</p> 
I		<p style="text-align: center;">$\frac{7}{10}$ Aaron</p> 
		<p>W- what I did is that I drew two boxes. On the top I labeled one $\frac{2}{3}$ and the other one $\frac{7}{10}$. In one box I colored in $\frac{2}{3}$. In the last box I shaded in $\frac{7}{10}$. For my equation I put "$\frac{2}{3} < \frac{7}{10}$."</p>
	E	$\frac{2}{3} < \frac{7}{10}$

Score Point: 1

The response to Part A is incorrect (0). The response to Part B includes a correct number sentence with incomplete explanation (1.5).

Instructional Materials Question 17

A ✓ - Is Maria correct or is she wrong?

I - ~~$\frac{3}{8}$~~ ~~$\frac{5}{8}$~~

E - $\frac{5 \times 3}{8 \times 3} = \frac{15}{24}$ = Maria
 $\frac{2 \times 8}{3 \times 8} = \frac{16}{24}$ = Cody (winner)

W - Is Maria correct or is she wrong? Maria is wrong. To solve this problem first I found a common denominator for the two fractions. I found out the common denominator was 24. From there I got two new new fractions they were $\frac{15}{24}$ and $\frac{16}{24}$. I knew $\frac{16}{24}$ is bigger. $\frac{16}{24}$ is the amount Cody read. Therefore I knew Maria was incorrect.

~~B~~

✓ - compare the number of pages cody and Aaron read using these symbols $>$, $<$, $=$.

I - $52 < 55$ or $1 > 0$ or $50 \geq 50$

E - $\frac{20}{30} < \frac{21}{30}$

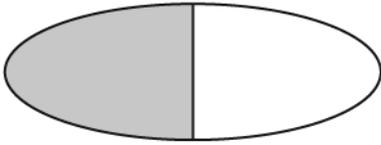
W -

Score Point: 1

The response to Part A includes some correct procedure (0.5). The response to Part B includes a correct number sentence with no work or explanation (1.0).

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.NF.A2

- 18** The weight of a box, in pounds, is **greater** than the fraction modeled by the diagram below.



Which of these could be the weight of the box? Select **all** that apply.

- A** $\frac{3}{5}$ pound
- B** $\frac{1}{4}$ pound
- C** $\frac{5}{6}$ pound
- D** $\frac{3}{4}$ pound
- E** $\frac{3}{8}$ pound

Scoring Notes:

Correct answers: A, C, D

Rationale B: denominator is greater

Rationale E: numerator and denominator are greater

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.NF.B3b

19 Which expressions have a value of $1\frac{5}{8}$?

Select **all** that apply.

A $\frac{8}{8} + \frac{1}{8} + \frac{1}{8} + \frac{2}{8}$

B $\frac{8}{8} + \frac{1}{8} + \frac{4}{8}$

C $\frac{1}{8} + \frac{2}{8} + \frac{3}{8}$

D $\frac{8}{8} + \frac{8}{8} + \frac{8}{8} + \frac{8}{8} + \frac{8}{8} + \frac{1}{8}$

E $\frac{8}{8} + \frac{1}{8} + \frac{1}{8} + \frac{1}{8} + \frac{1}{8} + \frac{1}{8}$

F $\frac{8}{8} + \frac{5}{8}$

Scoring Notes:

Correct answers: B, E, F

Rationale A: miscounts number of eighths

Rationale C: counts $\frac{1}{8}$ as 1 whole

Rationale D: reverses whole number and numerator

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.NF.B3c

20 What is $3\frac{2}{5} - 2\frac{3}{5}$? Write the answer as a fraction in the blank below.

Scoring Notes:

$\frac{4}{5}$ or equivalent

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.NF.B3d

21 Andrea used $\frac{7}{8}$ cup of flour when making 3 batches of cookies. Which expressions could show the number of cups of flour she used in **each** of the 3 batches of cookies she made? Select **all** that apply.

A $\frac{2}{8} + \frac{2}{8} + \frac{3}{8}$

B $\frac{1}{8} + \frac{1}{8} + \frac{2}{8} + \frac{3}{8}$

C $\frac{2}{8} + \frac{4}{8}$

D $\frac{3}{8} + \frac{4}{8} + \frac{0}{8}$

E $\frac{3}{8} + \frac{2}{8} + \frac{3}{8}$

Scoring Notes:

Correct answers: A, D

Rationale B: sums to $\frac{7}{8}$, but represents 4 batches

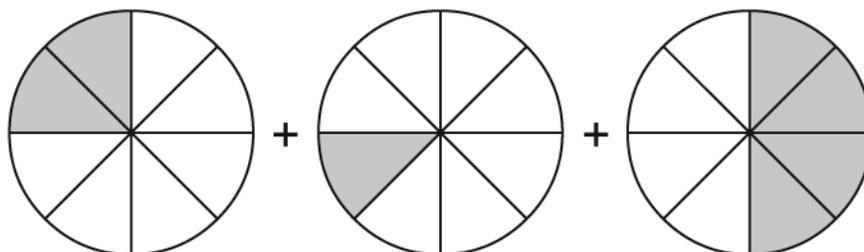
Rationale C: sums to $\frac{6}{8}$, but represents 2 batches

Rationale E: sums to $\frac{8}{8}$

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.NF.B3d

22

Three friends shared a pizza. Mary ate 2 slices and Ann ate 1 slice. Pete ate twice as many slices as Mary ate. The fraction model below represents the fraction of the pizza eaten by each of the friends.



What fraction of the pizza was eaten altogether? Show your work **and** explain your thinking.

Write your response on the grid below.

Scoring Notes:

For this item, a full-credit response (2 points) includes

- correct fraction of the pizza that was eaten by the three friends, $\frac{7}{8}$
- AND**
- correct work and explanation identifying the fraction of the pizza that was eaten by the three friends

For example,

- $\frac{2}{8} + \frac{1}{8} + \frac{4}{8} = \frac{7}{8}$

AND

The model shows that the pizza was divided into 8 slices. From the model, Mary ate $\frac{2}{8}$ and Ann ate $\frac{1}{8}$ of the pizza. Pete ate twice what Mary ate, so he ate $\frac{4}{8}$ of the pizza, which is also shown in the model.

Add all 3 fractions to get $\frac{7}{8}$ for the fraction of pizza eaten altogether.

For this item, a partial-credit response (1 point) includes

- correct fraction of the pizza that was eaten by the three friends, $\frac{7}{8}$

OR

- incorrect fraction due to a calculation error (work must be shown) with explanation identifying the fraction of pizza that was eaten by the three friends

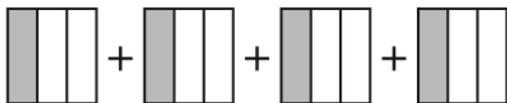
OR

- some work and explanation identifying the fraction of pizza that was eaten by the three friends

For this item, a no-credit response (0 points) includes none of the features of a full- or partial-credit response.

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.NF.B4a

23 A shaded fraction model is shown below.



Which equation shows the product represented by the shaded fraction model?

- A $2 \times \frac{1}{3} = \frac{2}{3}$
- B $3 \times \frac{1}{4} = \frac{3}{4}$
- C $4 \times \frac{1}{2} = \frac{4}{2}$
- D $4 \times \frac{1}{3} = \frac{4}{3}$

Scoring Notes:

Rationale A: multiplies number of rectangles by fraction of area shaded instead of number of shaded parts by fraction of area shaded

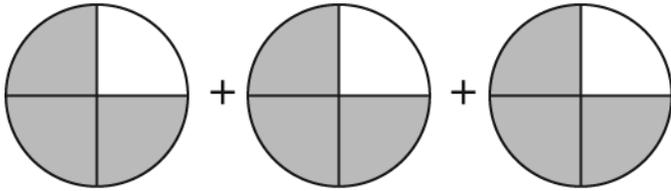
Rationale B: reverses whole number and denominator

Rationale C: uses number of rectangles as denominator instead of number of parts in each rectangle

Rationale D: correct

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.NF.B4b

24 A shaded fraction model is shown below.



When complete, the equation below can be used to describe the product of the shaded fraction model. Write a digit (0 through 9) in each box to complete the equation. A digit may be used in more than one box.

$$\square \times \frac{3}{\square} = \square \times \frac{1}{\square}$$

Scoring Notes:

$$3 \times \frac{3}{4} = 9 \times \frac{1}{4}$$

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.NF.B4c

- 25** Each of 5 friends drank $\frac{3}{4}$ pint of lemonade. Between which two whole numbers is the total number of pints of lemonade the friends drank? Show your work or explain your thinking.

Write your response on the grid below.

Scoring Notes:

For this item, a full-credit response (2 points) includes

- correct two whole numbers, 3 and 4
AND
- correct work showing how the two whole numbers were determined
OR
- explanation identifying how the two whole numbers were determined

For example,

- $\frac{3}{4} \times 5 = \frac{3}{4} \times \frac{5}{1} = \frac{15}{4} = 3\frac{3}{4}$

$$3\frac{3}{4} > 3$$

$$3\frac{3}{4} < 4$$

OR

- Multiply $5 \times \frac{3}{4}$ to find the total number of pints the friends drank. The five friends drank a total of $3\frac{3}{4}$ pints. And, $3\frac{3}{4}$ is between the whole numbers 3 and 4, since $3\frac{3}{4}$ is greater than 3, but less than 4.

For this item, a partial-credit response (1 point) includes

- correct two whole numbers, 3 and 4
OR
- incorrect whole numbers due to a calculation error (work must be shown for how the two whole numbers were determined)
OR
- some explanation identifying how the two whole numbers were determined

For this item, a no-credit response (0 points) includes none of the features of a full- or partial-credit response.

Nevada Instructional Materials Phase III

Grade 4 Mathematics

NVACS: M_4.NF.B4c; M_4.NF.A2

26

Calvin and Max raced using potato sacks. Calvin made 9 jumps. Each jump was $\frac{1}{3}$ foot in distance.

To find the total distance that he jumped, Calvin multiplied $\frac{1}{3}$ by 9. Calvin stated that he jumped a total distance of $\frac{9}{27}$ foot, but his answer is incorrect.

A What is the total distance, in feet, that Calvin jumped? Draw a picture to model your answer **and** explain why Calvin's answer is incorrect.

B Each jump Max made was $\frac{5}{12}$ foot. Did Calvin or Max jump the greater distance on **each** jump?

Show your work **and** explain your thinking.

Write your response on the grid on the next page.

Scoring Notes:

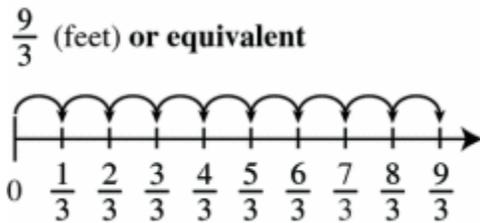
Score	Description
4	Student scores 4 points.
3	Student scores 3–3.5 points.
2	Student scores 2–2.5 points.
1	Student scores 0.5–1.5 points.
0	Student’s response provides insufficient evidence of appropriate skills or knowledge to successfully accomplish the task.
Blank	No student response.

Score Points

Part A:	score 2.0 points	correct answer and model with correct and complete explanation
	OR	
	score 1.5 points	correct answer and model with partially correct or incomplete explanation
	OR	
	score 1.0 point	correct answer with partially correct or incomplete explanation
	OR	correct model with partially correct or incomplete explanation
	OR	correct answer with correct and complete explanation
	OR	
	score 0.5 point	correct answer with no explanation
	OR	correct model with no explanation
Part B:	score 2.0 points	correct answer with correct and complete work and correct and complete explanation
	OR	
	score 1.5 points	correct answer with correct work and partially correct or incomplete explanation
	OR	correct and complete work and correct and complete explanation
	OR	
	score 1.0 point	correct answer with partially correct work and partially correct or incomplete explanation
	OR	
	score 0.5 point	correct answer with no work and explanation
	OR	partially correct or incomplete explanation
	OR	some correct procedure

Correct Answers

Part A:



AND

Sample Explanation:

Calvin jumped $\frac{1}{3}$ foot 9 times. As shown by the drawing, this is $\frac{9}{3}$, not $\frac{9}{27}$. Calvin multiplied both the numerator and the denominator by 3, instead of just the numerator.

Part B:

Max jumped the greater distance.

$$\frac{1}{3} = \frac{1 \times 4}{3 \times 4} = \frac{4}{12}$$

$$\frac{5}{12} > \frac{4}{12}$$

or equivalent work

AND

Sample Explanation:

Calvin jumped $\frac{4}{12}$ foot on each jump. Max jumped $\frac{5}{12}$ foot on each jump. Since $\frac{5}{12} > \frac{4}{12}$, Max jumped the greater distance on each jump.

No 4-point responses

Instructional Materials Question 26

A

$9 \times \frac{1}{3} = \frac{9}{3} = 3$ $\frac{1}{3} = 4 \text{ in}$ $3 \overline{)12}$

1 ft 2 ft 3 ft

$9 \times 4 = 36$

$\frac{1}{3} \frac{1}{3} \frac{1}{3} \frac{1}{3} \frac{1}{3} \frac{1}{3} \frac{1}{3} \frac{1}{3} \frac{1}{3} \frac{1}{3} = 1$

36
 12

Calvin jumped 3 feet or 36 in.

I know this because I divided and multiplied. First I tried I divided 12 by 3 to see how many inches is $\frac{1}{3}$. $\frac{1}{3}$ is 4 in. Second, I multiplied 9 by 4 and got a product of 36 in, or if you divide 36 by 12 you get 3 ft. Calvin's answer was wrong because he multiplied the fraction by the number.

B

Calvin = $\frac{1}{3}$ each jump = $\frac{4}{12}$

Max = $\frac{5}{12}$ each jump = $\frac{5}{12}$

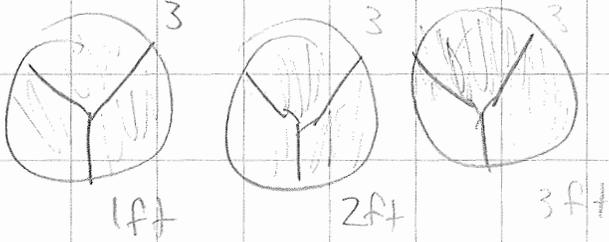
Max did the greatest distance because he did more than $\frac{1}{3}$ of a foot. I know this because I compared the two differences and put each fraction in the fraction of a foot.

Score Point: 3

The response to Part A includes the correct answer and model with incomplete explanation (1.5). The response to Part B includes the correct answer with correct and complete work and correct and complete explanation (2.0).

Instructional Materials Question 26

A



Calvin's answer was incorrect because 3 of the nine jumps would equal a foot in distance, $9 \times \frac{1}{3} = \frac{13}{3}$ or $\frac{1}{1}$. He would end up with 3 whole feet.

B

$$\frac{1}{3} > \frac{4}{12} \otimes \frac{5}{12}$$

First you have to get each to the same denominator. I turned $\frac{1}{3}$ into $\frac{4}{12}$ by multiplying each number in $\frac{1}{3}$ by 4. $\frac{5}{12}$ is greater than $\frac{4}{12}$, so Max jumped farther.

Score Point: 3

The response to Part A includes the correct answer and model with incomplete explanation (1.5). The response to Part B includes the correct answer with correct and complete work and correct and complete explanation (2.0).

Instructional Materials Question 26

A

Calvin Jumped 3 feet
because nine times one
third is 3.

$$9 \times \frac{1}{3} = \frac{9}{3}$$

$$\begin{array}{r} 3 \\ \overline{)9} \\ 9 \\ \hline 0 \end{array}$$

B

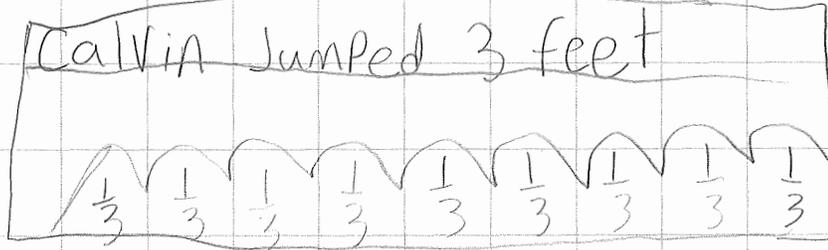
Max Jumped farther than
calvin because $\frac{4}{10}$
greater than one third.

Score Point: 2

The response to Part A includes the correct answer with incomplete explanation (1.0). The response to Part B includes the correct answer with incomplete work/explanation (1.0).

Instructional Materials Question 26

A



The total distance, in feet was 3 feet. Calvin's answer is incorrect because if you make 9 jumps that $\frac{1}{3}$ each then you keep the denominator the same and just add the numerators which is $\frac{9}{3}$. $3 \frac{9}{3}$ 3 feet

B

Calvin jumped the greater distance because 3 is a whole number and whole numbers are bigger than $\frac{5}{12}$.

Score Point: 2

The response to Part A includes the correct answer and model with correct and complete explanation (2.0). The response to Part B is incorrect (0).

Instructional Materials Question 26

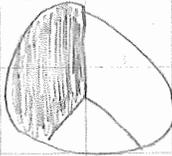
A



What I did was I drew 3 circles and cut them up in to 3rds and colored in each time he made a jump and I got 3 whole circles.

fractions	
$\frac{1}{3}$	$\frac{5}{12}$

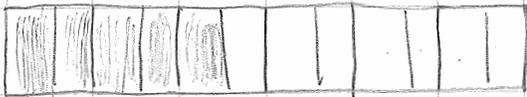
Calvin



Max had the greatest distance because 12 is bigger than 3 and 5 is bigger than 1.

B

max



Score Point: 1

The response to Part A includes a correct model with incomplete explanation (1.0). The response to Part B includes the correct answer, but for the wrong reason, and represents a common error in student work (0).

Instructional Materials Question 26

A

$\frac{1}{3}$
 $\times \frac{9}{9}$

 $\frac{9}{9} = 3$

Wrong.

B

$\frac{1}{3} \times \frac{4}{12}$
 $\frac{4}{36}$

$\frac{4}{6} \times \frac{5}{12}$
 $\frac{20}{72}$

Score Point: 1

The response to Part A includes the correct answer with no model or explanation (0.5). The response to Part B includes some correct procedure (0.5).

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.NF.C5

27

Select true or false for **each** equation below.

A $\frac{6}{10} + \frac{2}{100} = \frac{62}{100}$

True False

B $\frac{2}{10} + \frac{8}{100} = \frac{10}{100}$

True False

C $\frac{6}{100} + \frac{1}{10} = \frac{16}{100}$

True False

D $\frac{3}{100} + \frac{4}{10} = \frac{34}{100}$

True False

Scoring Notes:

True: A, C

False: B, D

Rationale B: did not notice different denominators of addends

Rationale D: combined numerators (similar to option A) but did not look at denominator of each addend

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.NF.C6

28 Which decimal number is equivalent to $\frac{54}{100}$?

- A 0.0054
- B 0.054
- C 0.54
- D 5.4

Scoring Notes:

Rationale A: put two zeros in front of 54 because dividing by 100, which has two zeros

Rationale B: $\frac{54}{1000}$

Rationale C: correct

Rationale D: $\frac{54}{10}$

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.NF.C6

29 Marco has read 0.05 of the pages in his book. Use the bar below to write the fraction of the pages in his book that Marco has read.

Scoring Notes:

$\frac{5}{100}$

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.NF.C7

30

Four incomplete number sentences and 5 digits are shown in the table below.

Number Sentence	1	2	4	5	8
$3.7 < 3.\square$					
$9.04 > 9.0\square$					
$4.5\square = 4.52$					
$2.65 > 2.\square 6$					

Put a mark in the box below **each** digit that can be used to complete **each** number sentence and make it true.

Scoring Notes:

Number Sentence	1	2	4	5	8
$3.7 < 3.\square$					x
$9.04 > 9.0\square$	x	x			
$4.5\square = 4.52$		x			
$2.65 > 2.\square 6$	x	x	x	x	

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.MD.A1

31 A conversion table for some numbers of pounds and ounces is shown below.

Pounds and Ounces

Number of Pounds	Number of Ounces
2	
4	
6	
8	

Complete the table by writing the number of ounces in each number of pounds.

Scoring Notes:

Pounds and Ounces

Number of Pounds	Number of Ounces
2	32
4	64
6	96
8	128

Nevada Instructional Materials Phase III

Grade 4 Mathematics

NVACS: M_4.MD.A2; M_4.MD.A1

32

The distances, in **kilometers**, that Kurt rode his bike on Saturday and Sunday are shown below.

- Saturday: 17.2 kilometers
- Sunday: 14.8 kilometers

What is the total distance, in **meters**, that Kurt rode his bike on Saturday and Sunday?

- A** 32 meters
- B** 320 meters
- C** 3200 meters
- D** 32000 meters

Scoring Notes:

Rationale A: did not convert to meters

Rationale B: converted incorrectly to meters

Rationale C: converted incorrectly to meters

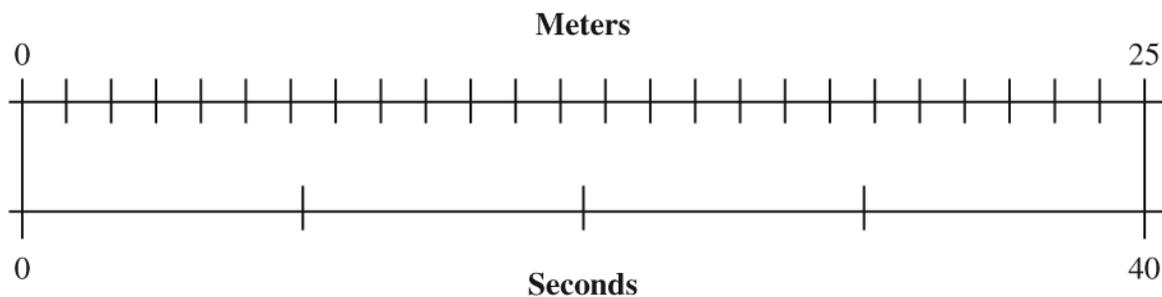
Rationale D: correct

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.MD.A2; M_4.MD.A1

33

Jesse is practicing for a swimming competition. She swims 25 meters in 40 seconds.

- A** Using the double number line diagram on the next page, find about how many meters Jesse swims in 10 seconds. Explain your thinking.



- B** To qualify for the swimming competition, Jesse must be able to swim 1 **kilometer** in no more than 30 **minutes**.

Using this information, explain why Jesse should be able to qualify for the swimming competition.

Write your response on the grid on the next page.

Scoring Notes:

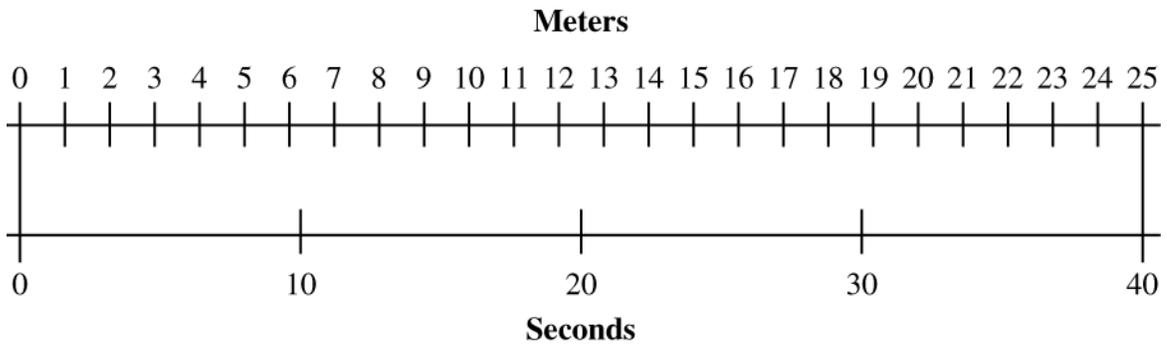
Score	Description
3	Student scores 3 points.
2	Student scores 2–2.5 points.
1	Student scores 0.5–1.5 points.
0	Student’s response provides insufficient evidence of appropriate skills or knowledge to successfully accomplish the task.
Blank	No student response.

Score Points

Part A:	score 1.5 points	correct number line with correct and complete explanation
	OR	
	score 1.0 point	correct number line with partially correct or incomplete explanation
	OR	partially correct or incomplete number line with correct and complete explanation
OR		
	score 0.5 point	correct number line with no explanation
	OR	partially correct or incomplete explanation
	OR	partially correct or incomplete number line with no explanation
	OR	some correct procedure
Part B:	score 1.5 points	correct and complete explanation
	OR	
	score 1.0 point	partially correct or incomplete explanation
	OR	
	score 0.5 point	vague explanation only
	OR	some correct procedure

Correct Answers

Part A: The response shows a correct number line diagram.



AND

Sample Explanation:

I located where 10 seconds is on the bottom line of the diagram and looked right above it to find how many meters Jesse swims. Jesse swims a little more than 6 meters in 10 seconds.

Part B: Accept all correct and complete explanations.

Sample Explanation:

1000 meters is equal to one kilometer and 60 seconds equals 1 minute.

So, Jesse has to be able to swim 1000 meters in $30 \times 60 = 1800$ seconds.

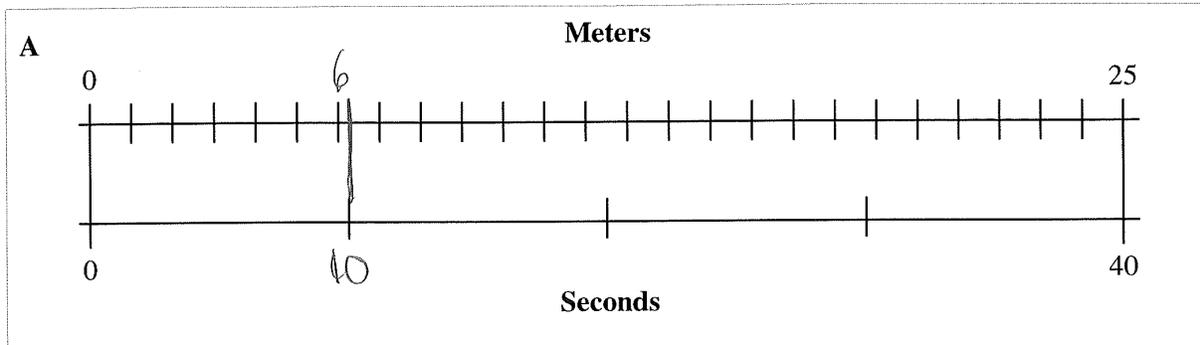
$$1000 \div 25 = 40$$

Swimming at the same speed, it would take her $40 \times 40 = 1600$ seconds to swim 1000 meters.

Since 1600 is less than 1800, she should be able to qualify.

No 3-point responses

Instructional Materials Question 33



Jesse does around 6 m
in 10 seconds.

B Jesse would be able to
complete a kilometer
in about 26 min, and 40 sec.

$$\begin{array}{r} 40 \\ 25 \overline{)1000} \\ \underline{1000} \\ 00 \end{array}$$

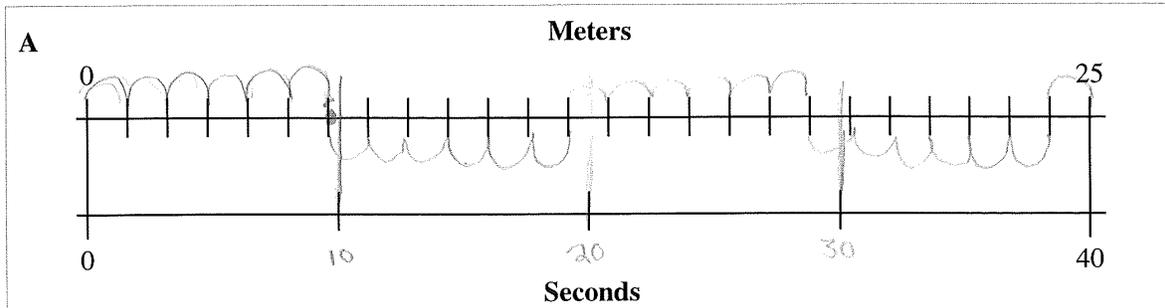
$$\begin{array}{r} 40 \\ \times 40 \\ \hline 1600 \end{array}$$

$$\begin{array}{r} 26 \\ 60 \overline{)1600} \\ \underline{120} \downarrow \\ 400 \\ \underline{360} \\ 40 \end{array}$$

Score Point: 2

The response to Part A includes an incomplete number line with no explanation (0.5). The response to Part B includes a correct and complete explanation (1.5).

Instructional Materials Question 33



Every ten seconds, Jesse swims about 6 meters. I know this because the closest mark to the ten second line is the mark for the number six.

B

25m in 40s
1000m in 1800s

$$\begin{array}{r} 450 \\ 4 \overline{)1800} \\ \underline{16} \\ 20 \\ \underline{20} \\ 00 \end{array}$$

$$\begin{array}{r} 40 \\ 25 \overline{)1000} \\ \underline{100} \\ 00 \end{array}$$

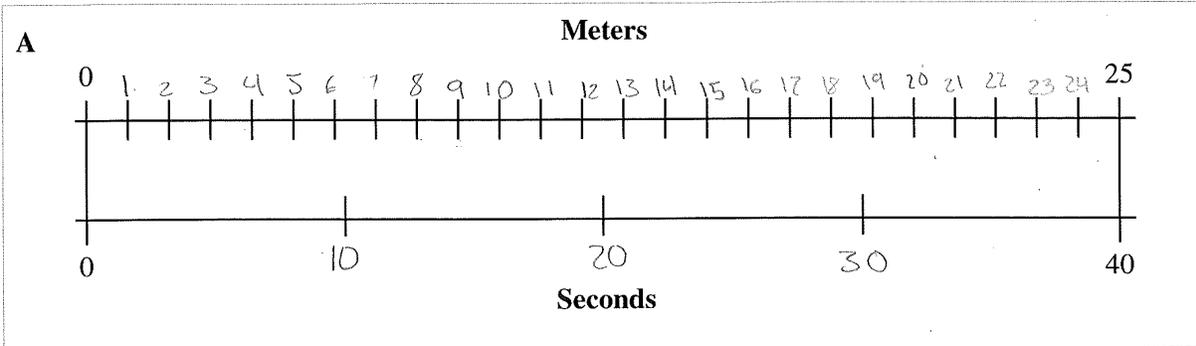
$$\begin{array}{r} 30 \\ 260 \\ \underline{1800} \end{array}$$

Jesse will be able to qualify for the swimming competition, because 25 meters is equal to 1000 meters, and 40 seconds is equal to 1800 seconds. I know this because I divided 1000 by 25 and 1800 by 40, and got an even amount. To conclude, Jesse should be able to qualify.

Score Point: 2

The response to Part A includes a correct number line with correct and complete explanation (1.5). The response to Part B includes some correct procedure (0.5).

Instructional Materials Question 33



I filled in the chart. The seconds go by 10 and the meters go by ones. Then I looked at 10 and went up and the answer is $6\frac{2}{3}$.

B

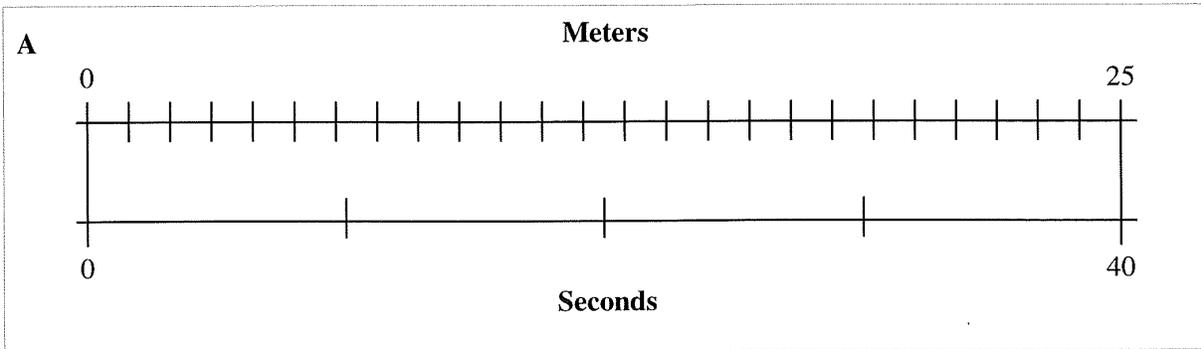
$$\begin{array}{r}
 30 \\
 \underline{60} \\
 00 \\
 + 180 \\
 \hline
 180
 \end{array}
 \qquad
 \begin{array}{r}
 40 \overline{) 180} \\
 \underline{40} \\
 00 \\
 \underline{40} \\
 00 \\
 \underline{40} \\
 00 \\
 \underline{40} \\
 00
 \end{array}$$

Jesse will be able to qualify because she will be able to do more than 1 kilometer. She will be able to at least do 4.

Score Point: 1

The response to Part A includes a correct number line with correct and complete explanation (1.5). The response to Part B is incorrect (0).

Instructional Materials Question 33



He swims around 6 meters each 10 seconds.

B Jesse will make 1 kilometer because he has a long time to make it.

Score Point: 1

The response to Part A includes some correct procedure (0.5). The response to Part B is incorrect (0).

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.MD.A3; M_4.OA.B4

34 The length and width of a rectangle are each a whole number of inches. The perimeter of the rectangle is 40 inches. Which of these could be the area of the rectangle? Select **all** that apply.

- A** 36 square inches
- B** 51 square inches
- C** 68 square inches
- D** 75 square inches
- E** 80 square inches
- F** 100 square inches

Scoring Notes:

Correct answers: A, B, D, F

Rationale C: thinks all multiples of 4 could be the area

Rationale E: doubles perimeter

For this item, a partial-credit response (1 point) includes

- correct number of miles, $1\frac{3}{4}$ (miles)

OR

- incorrect number of miles due to a calculation error (work must be shown)

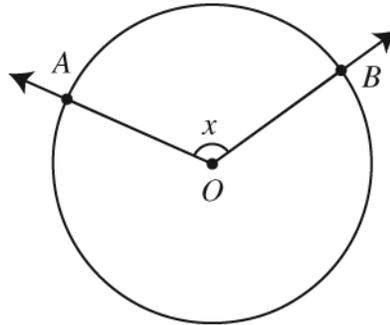
OR

- some explanation indicating how the total number of miles was determined

For this item, a no-credit response (0 points) includes none of the features of a full- or partial-credit response.

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.MD.C5a

36 Ray OA and ray OB meet at the center of circle O to form angle AOB , as shown below.



Exactly $\frac{1}{3}$ of circle O lies within angle AOB . What is the measure (x) of angle AOB ?

- A 30°
- B 60°
- C 120°
- D 180°

Scoring Notes:

Rationale A: 3 in denominator of fraction

Rationale B: common angle measurement

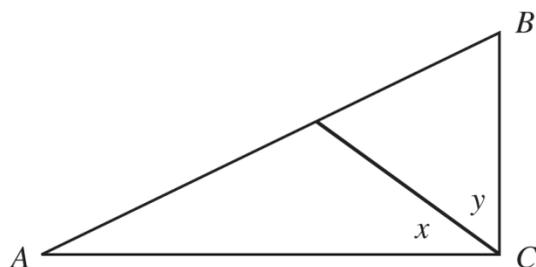
Rationale C: correct

Rationale D: estimates half a circle; common angle measurement

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.MD.C7

37

In triangle ABC , shown below, the measure of angle ACB is 90° .



Which of these could be the measures of x and y ? Select **all** that apply.

- A** $x = 30^\circ$ and $y = 55^\circ$
- B** $x = 45^\circ$ and $y = 45^\circ$
- C** $x = 60^\circ$ and $y = 30^\circ$
- D** $x = 20^\circ$ and $y = 40^\circ$
- E** $x = 17^\circ$ and $y = 73^\circ$
- F** $x = 23^\circ$ and $y = 57^\circ$

Scoring Notes:

Correct answers: B, C, E

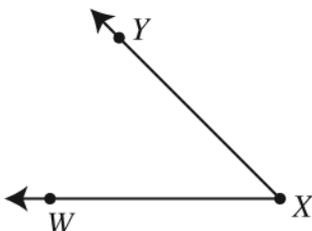
Rationale A: sum of 85°

Rationale D: sum of 60°

Rationale F: sum of 80°

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.MD.C6

- 38** Angle WXY is shown in the diagram below. Using a measuring tool, draw angle WXZ on the diagram so that angle WXZ measures 100° more than angle WXY . Explain how you got your answer.



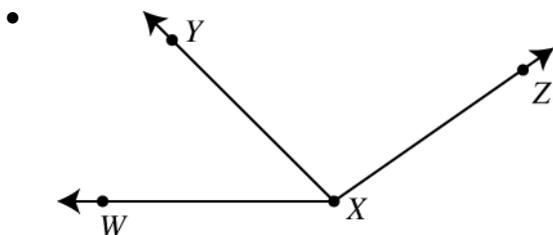
Write your response on the grid below.

Scoring Notes:

For this item, a full-credit response (2 points) includes

- correct angle measure for angle WXZ , 145° , with point Z labeled on ray **AND**
- explanation indicating how angle WXZ was determined

For example,



AND

I measured angle WXY as 45° , so angle WXZ has to measure 145° . So I drew angle WXZ measuring 145° .

OR

Since angle WXZ measures 100° more than angle WXY , I needed to add a 100° angle onto angle WXY . So I drew a 100° angle with ray XY as one of its sides.

For this item, a partial-credit response (1 point) includes

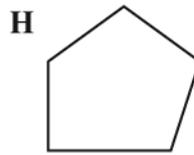
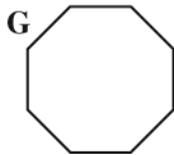
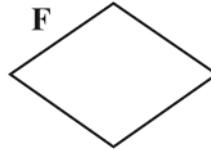
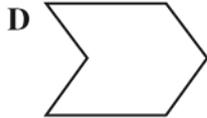
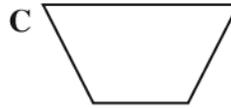
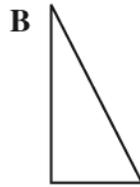
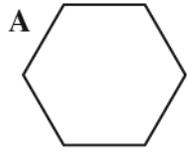
- correct angle measure for angle WXZ , 145° , with point Z labeled on ray **OR**
- some explanation indicating how angle WXZ was determined **OR**
- angle WXZ drawn within $\pm 0.5^\circ$, with point Z labeled on ray

For this item, a no-credit response (0 points) includes none of the features of a full- or partial-credit response.

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.G.A1

39

Circle **each** shape below that appears to contain perpendicular line segments.



Scoring Notes:

Correct answers: B, E, H

Rationale A: confuses perpendicular and parallel

Rationale C: confuses perpendicular and parallel

Rationale D: confuses perpendicular and parallel

Rationale F: confuses perpendicular and parallel

Rationale G: confuses perpendicular and parallel

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.G.A1; M_4.G.A2

40 Anusha drew 4 line segments to make a quadrilateral with 2 right angles, 1 acute angle, and 1 obtuse angle.

Draw a quadrilateral that could look like the quadrilateral Anusha drew. Write the name that **best** describes the quadrilateral you drew, and use the relationship between the sides of the quadrilateral to explain your thinking.

Write your response on the grid below.

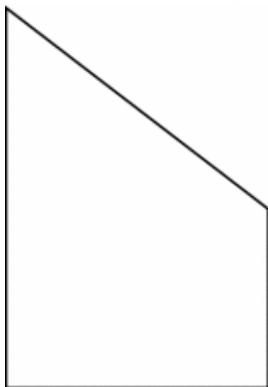
Scoring Notes:

For this item, a full-credit response (2 points) includes

- correct drawing of the quadrilateral
AND
- correct name of the quadrilateral drawn, trapezoid
AND
- explanation using the relationship between the sides of the quadrilateral

For example,

- student draws a trapezoid similar to:



AND

- The figure is a trapezoid because at least one pair of sides is parallel.

For this item, a partial-credit response (1 point) includes

- correct drawing of the quadrilateral
OR
- correct name of the quadrilateral drawn, trapezoid
OR
- some explanation using the relationship between the sides of the quadrilateral

For this item, a no-credit response (0 points) includes none of the features of a full- or partial-credit response.

(Note: A trapezoid is defined as having at least one pair of parallel sides.)

Nevada Instructional Materials Phase III

Grade 4 Mathematics

NVACS: M_4.G.A.2; M_4.G.A.1

41 Angle x is labeled in the rectangle shown below.



What type of angle is angle x ?

- A acute
- B obtuse
- C parallel
- D right

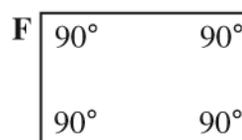
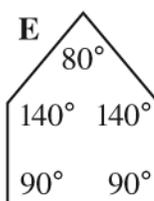
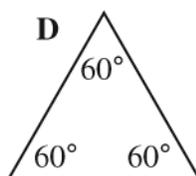
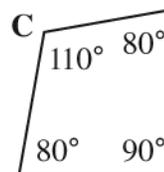
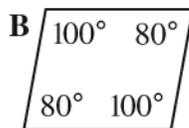
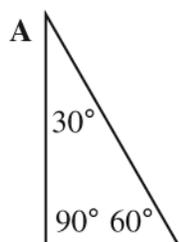
Scoring Notes:

- Rationale A:** confuses acute and right angles
- Rationale B:** confuses obtuse and right angles
- Rationale C:** familiar term
- Rationale D:** correct

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.G.A2

42

Circle **all** the figures below that can be classified as parallelograms.



Scoring Notes:

Correct answers: B, F

Rationale A: thinks 90° angle implies parallelogram

Rationale C: thinks some opposite angles of equal measure implies parallelogram

Rationale D: thinks all angles of equal measure implies parallelogram

Rationale E: contains some parallel segments

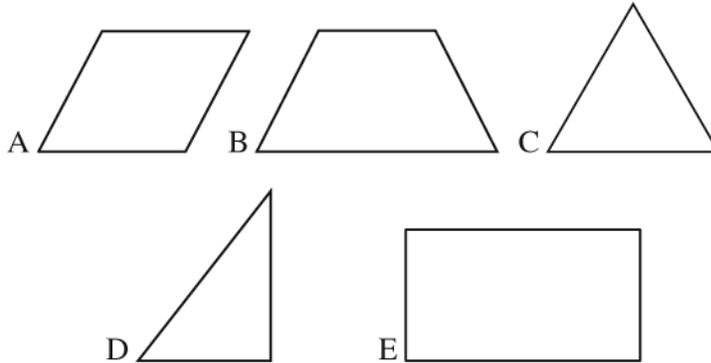
Nevada Instructional Materials Phase III

Grade 4 Mathematics

NVACS: M_4.G.A.2; M_4.G.A.1

43

Five shapes are shown below.



- A** Complete the table on the next page by placing check marks in each row to describe whether the shape appears to have parallel sides and/or perpendicular sides. Check **all** that apply.
- B** Name a shape that has **both** parallel and perpendicular sides that is **not** shown above or described in the table. Explain your thinking.

Write your response on the grid on the next page.

Scoring Notes:

Score	Description
3	Student scores 3 points.
2	Student scores 2–2.75 points.
1	Student scores 0.25–1.5 points.
0	Student’s response provides insufficient evidence of appropriate skills or knowledge to successfully accomplish the task.
Blank	No student response.

Score Points

Part A:	score 1.5 points	correct and complete table deduct 0.25 point for each incorrect check mark (maximum deduction 1.5 points)
Part B:	score 1.5 points OR score 1.0 point OR score 0.5 point	correct answer (answers may vary) with correct and complete explanation correct answer (answers may vary) with partially correct or incomplete explanation correct answer (answers may vary) with no explanation OR partially correct, vague, or incomplete explanation OR some correct procedure

Correct Answers

Part A: Correct and complete table.

Shape	Parallel Sides	Perpendicular Sides
A	✓	
B	✓	
C		
D		✓
E	✓	✓

Part B: Answers may vary.

Sample Answer and Explanation:

Square

It can be a square because a rectangle is already shown. I know squares (as well as rectangles) have both perpendicular and parallel sides because the angles formed at each corner are 90° (definition of perpendicular) and because the distance between the opposite sides is always the same distance apart and the sides will never meet (definition of parallel).

OR

Trapezoid

It can be a different trapezoid than the one shown. This trapezoid could have 2 angles that measure 90° . The trapezoid would have sides that are perpendicular because of the 90° angles (definition of perpendicular), and it would have sides that are parallel because the angles between them are equal, which means the sides will never meet (definition of parallel).

(Note: Student could name any shape [e.g., pentagon, hexagon] if the figure contains 2 angles that measure 90° as described above.)

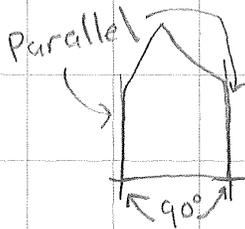
(Note: A trapezoid is defined as having at least one pair of parallel sides.)

Instructional Materials Question 43

A

Shape	Parallel Sides	Perpendicular Sides
A	2	0
B	1	0
C	0	0
D	0	1
E	2	4

B



A shape that has parallel and Perpendicular sides and are not any of the five shapes is a Pentagon. It has 2 perpendicular sides that make a 90° angle. It also has parallel lines on the sides.

Score Point: 3

The response to Part A includes a correct and complete table (parallel column counts pairs of sides; perpendicular column counts right angles) (1.5). The response to Part B includes a correct answer with correct and complete explanation (1.5).

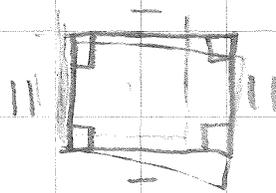
Instructional Materials Question 43

A

Shape	Parallel Sides	Perpendicular Sides
A	✓	
B	✓	
C		
D	✓	✓
E	✓	✓

B

A square because all the sides are the same length and it is like a rectangle.



Score Point: 2

The response to Part A includes a correct and complete table (1.5). The response to Part B includes a correct answer with incomplete explanation (1.0).

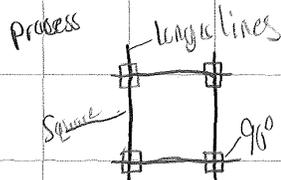
Instructional Materials Question 43

A

Shape	Parallel Sides	Perpendicular Sides
A	✓	
B		
C		
D		✓
E	✓	✓

B

I see a shape on this graph paper. I is the squares. A perpendicular side is when they all have degrees of 90°. If you draw the lines longer, you will see ninety degrees.



Score Point: 2

The response to Part A includes a table with missing check mark for shape B (1.25). The response to Part B includes a correct answer with incomplete explanation (1.0).

Instructional Materials Question 43

A

Shape	Parallel Sides	Perpendicular Sides
A	✓	
B	✓	
C		
D		✓
E	✓	✓

B

Explanation: The rectangular (shape E) has parallel lines and perpendicular lines. I know this because I used pictures and a table. First, I checked all the shapes that had parallel sides or perpendicular sides, then I recorded it on the table. After that, I saw that a rectangle has parallel sides and perpendicular sides.

Score Point: 1

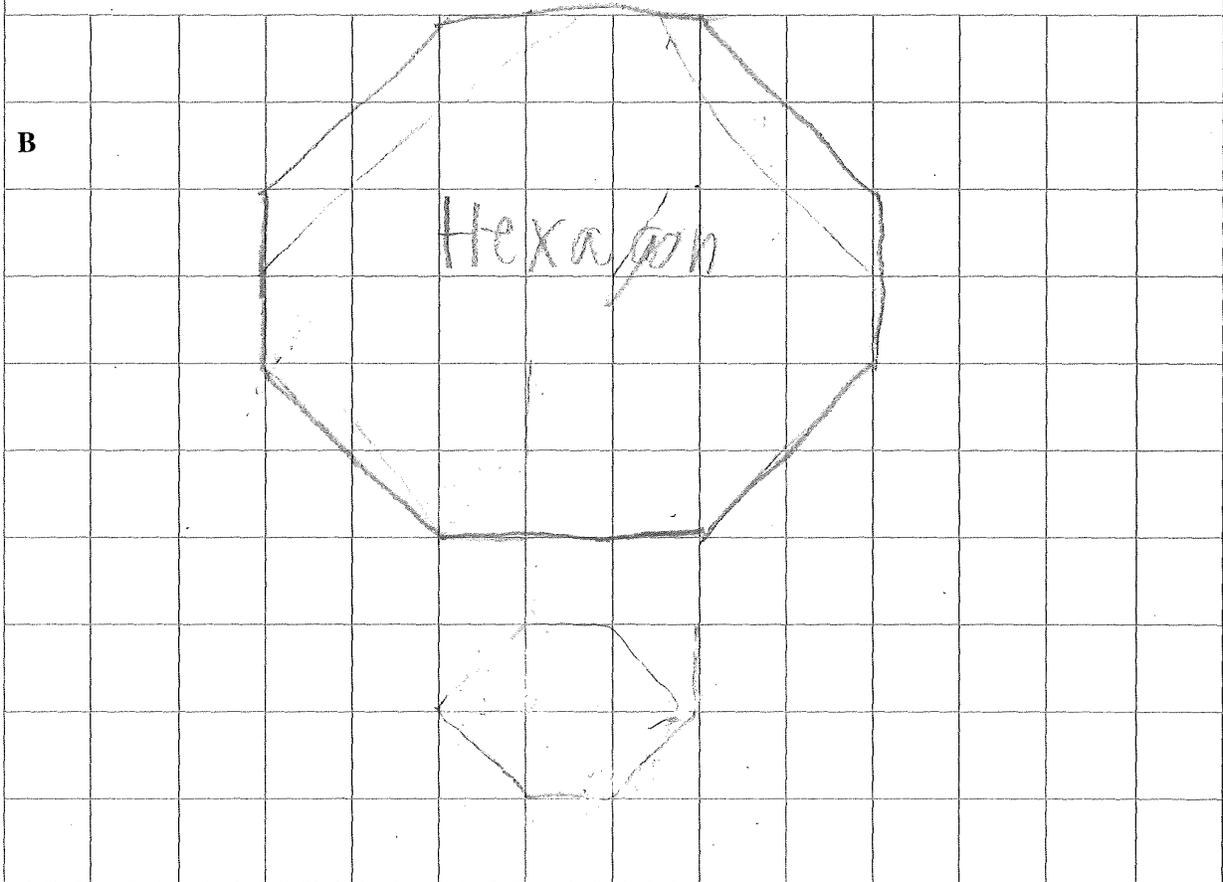
The response to Part A includes a correct and complete table (1.5). The response to Part B is incorrect (0).

Instructional Materials Question 43

A

Shape	Parallel Sides	Perpendicular Sides
A	✓	
B	✓	
C		✓
D		✓
E	✓	

B



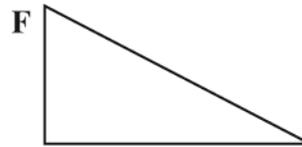
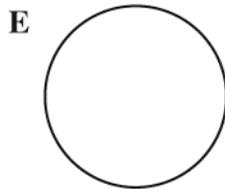
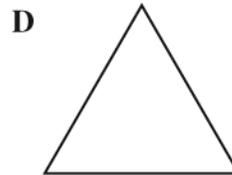
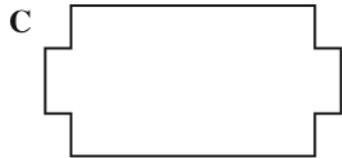
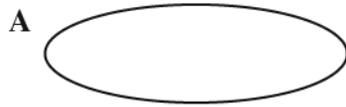
Score Point: 1

The response to Part A includes a table with additional check mark for shape C and missing check mark for shape E (1.0). The response to Part B is incorrect (0).

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.G.A.3

44

Circle each figure below on which **more** than 1 line of symmetry could be drawn.



Scoring Notes:

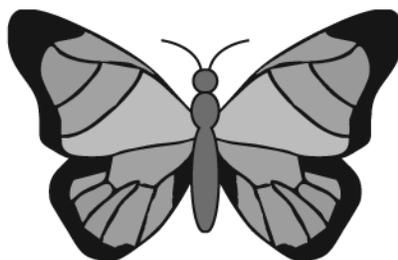
Correct answers: A, C, D, E

Rationale B: only 1 line of symmetry

Rationale F: no lines of symmetry

Nevada Instructional Materials Phase III
Grade 4 Mathematics
NVACS: M_4.G.A3

45 A picture of a butterfly is shown below.



Draw all lines of symmetry on the butterfly. Explain how you know your answer is correct.

Write your response on the grid below.

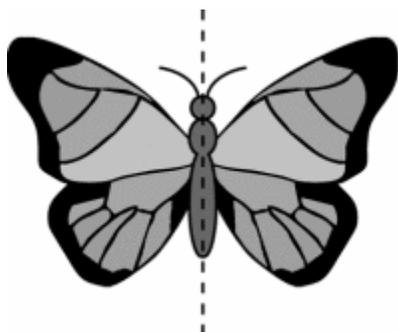
Scoring Notes:

For this item, a full-credit response (2 points) includes

- correct line of symmetry drawn on the picture of the butterfly
AND
- correct explanation indicating why only one line is drawn on the picture

For example,

•



AND

- The only line of symmetry goes down the center vertically because this is the only way you can fold the figure in half on this line and have all the sides match up. There is no horizontal line of symmetry because if you folded horizontally the top wings are bigger than the bottom. Similarly, a diagonal line wouldn't work because the large wings would not match up with the opposite small wings. So there is only one line of symmetry on this shape, as I have drawn.

For this item, a partial-credit response (1 point) includes

- correct line of symmetry drawn on the picture of the butterfly
- OR**
- some explanation indicating why only one line is drawn on the picture

For this item, a no-credit response (0 points) includes none of the features of a full- or partial-credit response.



Dale A.R. Erquiaga

Superintendent of Public Instruction

Office of Assessment, Program Accountability, and Curriculum

775-687-9188

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Grade 4**